

$$\sin x - \sin 15x \cdot \cos x = 3/2$$

$$\sin x - \sin 15x \cdot \cos x =$$

$$= \sqrt{1 + \sin^2(15x)} \left[\sin x \cdot \frac{1}{\sqrt{1 + \sin^2(15x)}} + \cos x \cdot \frac{-\sin 15x}{\sqrt{1 + \sin^2(15x)}} \right] = \sqrt{1 + \sin^2(15x)} [\sin x \cdot \cos t + \cos x \cdot \sin t] = \sqrt{1 + \sin^2(15x)} \sin(x+t)$$

$$\sqrt{1 + \sin^2(15x)} \sin(x+t) = 3/2$$

Решения нет

Тк левая часть макс равна $\sqrt{2}$, а пр $1,5 \Rightarrow$ они не

равны

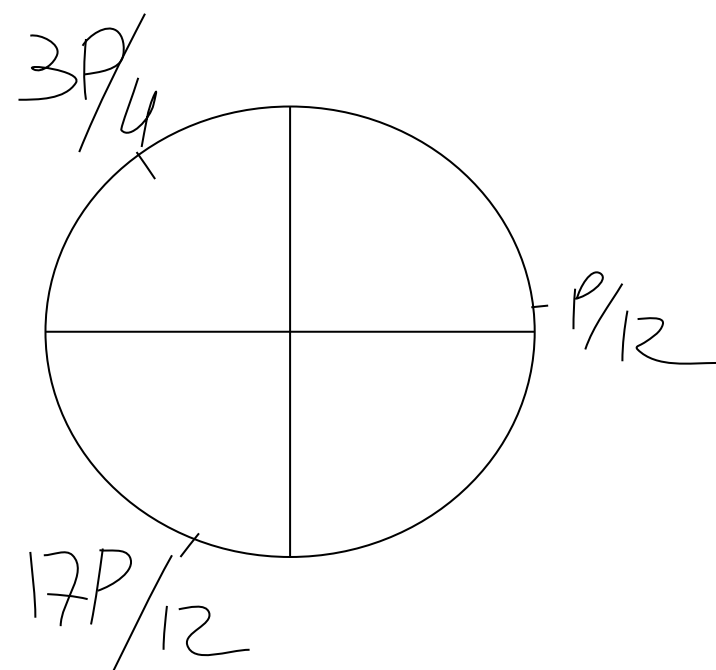
$$\cos t = 1/\sqrt{1 + \sin^2(15x)}$$

$$\sin t = -\sin 15x/\sqrt{1 + \sin^2(15x)}$$

подсказка

$$A \sin x + B \cos x = 3/2$$

$$A=1 \quad B=-\sin 15x$$



$$\sin 3x - 2\sin 18x \cdot \sin x = 3\sqrt{2} - \cos 3x + 2\cos x$$

$$\sin 3x + \cos 3x = 3\sqrt{2} + 2\sin 18x \cdot \sin x + 2\cos x$$

$$\sqrt{2}[\sin 3x \cdot 1/\sqrt{2} + \cos 3x \cdot 1/\sqrt{2}] = \sqrt{2}[\sin 3x \cdot \cos P/4 + \cos 3x \cdot \sin P/4] = \sqrt{2} \sin(3x + P/4)$$

$$\cos t = 1/\sqrt{2}$$

$$\sin t = 1/\sqrt{2}$$

$$t = P/4$$

$$2\sin 18x \cdot \sin x + 2\cos x = \sqrt{4 + 4\sin^2(18x)} \left[\sin x \cdot \frac{2\sin 18x}{\sqrt{4 + 4\sin^2(18x)}} + \cos x \cdot \frac{2}{\sqrt{4 + 4\sin^2(18x)}} \right] =$$

$$= \sqrt{4 + 4\sin^2(18x)} [\sin x \cdot \cos t + \cos x \cdot \sin t] = \sqrt{4 + 4\sin^2(18x)} \sin(x+t)$$

$$\cos t = 2\sin 18x/\sqrt{4 + 4\sin^2(18x)}$$

$$\sin t = 2/\sqrt{4 + 4\sin^2(18x)}$$

$$\sqrt{2} \sin(3x + P/4) = 3\sqrt{2} + \sqrt{4 + 4\sin^2(18x)} \sin(x+t)$$

$$\sqrt{2} \sin(3x + P/4) = 3\sqrt{2} + 2\sqrt{1 + \sin^2(18x)} \sin(x+t)$$

Оценка левой части

$$-1 \leq \sin(3x + P/4) \leq 1 \quad | \cdot \sqrt{2}$$

$$-\sqrt{2} \leq \sqrt{2} \sin(3x + P/4) \leq \sqrt{2}$$

Оценка правой части

$$-1 \leq \sin(18x) \leq 1$$

$$0 \leq \sin^2(18x) \leq 1 \quad | +1$$

$$1 \leq \sin^2(18x) + 1 \leq 2 \quad | \cdot \sqrt{2}$$

$$1 \leq \sqrt{2}(\sin^2(18x) + 1) \leq \sqrt{2} \quad | \cdot 2$$

$$2 \leq 2\sqrt{2}(\sin^2(18x) + 1) \leq 2\sqrt{2}$$

$$-1 \leq \sin(x+t) \leq 1$$

$$2\sqrt{2} \geq 2\sqrt{2}(\sin^2(18x) + 1) \sin(x+t) \geq -2\sqrt{2} \quad | +3\sqrt{2}$$

$$\sqrt{2} \leq 2\sqrt{2}(\sin^2(18x) + 1) \sin(x+t) + 3\sqrt{2} \leq 5\sqrt{2}$$

$$\sqrt{2} \sin(3x + P/4) = \sqrt{2}$$

$$\sin(3x + P/4) = 1$$

$$3x + P/4 = P/2 + 2Pk$$

$$x = P/6 + 2Pk/3 - P/12$$

$$x = P/12 + 2Pk/3$$

Проверяем 3 найденные точки в пр части

$$x = P/12$$

$$3\sqrt{2} + 2\sin(18P/12) \cdot \sin P/12 + 2\cos P/12 =$$

$$= 3\sqrt{2} + 2\sin 3P/2 \cdot \sin P/12 + 2\cos P/12 =$$

$$= 3\sqrt{2} - 2\sin P/12 + 2\cos P/12$$

$$2\cos P/12 - 2\sin P/12 = \sqrt{8}[\cos P/12 \cdot 2/\sqrt{8} - \sin P/12 \cdot 2/\sqrt{8}] = \sqrt{8}[\cos P/12 \cdot \sin P/4 - \sin P/12 \cdot \cos P/4] = \sqrt{8} \sin(P/4 - P/12) = \sqrt{8} \sin P/6$$

$$\cos t = 2/\sqrt{8} = 1/\sqrt{2} = \sqrt{2}/2$$

$$\sin t = 2/\sqrt{8} = 1/\sqrt{2} = \sqrt{2}/2$$

$$t = P/4$$

$$\sqrt{8} \sin P/6 = 2\sqrt{2}/2 = \sqrt{2}$$

Пр часть равна $4\sqrt{2} \Rightarrow x = P/12$ не подходит

$$x = 3P/4$$

$$3\sqrt{2} + 2\sin 54P/4 \cdot \sin 3P/4 + 2\cos 3P/4 =$$

$$= 3\sqrt{2} + \sqrt{2} \sin 27P/2 - \sqrt{2} = \sqrt{2} \sin 27P/2 + 2\sqrt{2} =$$

$$= \sqrt{2} \sin 3P/2 + 2\sqrt{2} = -\sqrt{2} + 2\sqrt{2} = \sqrt{2}$$

$$x = 17P/12$$

$$3\sqrt{2} + 2\sin(3 \cdot 17P/2) \cdot \sin 17P/12 + 2\cos 17P/12 =$$

$$= 3\sqrt{2} + 2\sin 3P/2 \cdot \sin 17P/12 + 2\cos 17P/12 =$$

$$3\sqrt{2} - 2\sin 17P/12 + 2\cos 17P/12$$

$$2\cos 17P/12 - 2\sin 17P/12 = \sqrt{8}[\cos 17P/12 \cdot 2/\sqrt{8} -$$

$$-\sin 17P/12 \cdot 2/\sqrt{8}] = \sqrt{8}[\cos 17P/12 \cdot \sin t - \sin 17P/12 \cdot \cos t] =$$

$$= \sqrt{8} \sin(17P/12 - P/4) = \sqrt{8} \sin(14P/12) = \sqrt{8} \sin(7P/6) =$$

$$= -\sqrt{8}/2 = -\sqrt{2}$$

$$t = P/4$$

$$-\sqrt{2} + 3\sqrt{2} = 2\sqrt{2}$$

Пр часть равна $2\sqrt{2} \Rightarrow x = 17P/12$ не подходит

Ответ: $3P/4 + 2Pk$